



SNS COLLEGE OF TECHNOLOGY



Coimbatore-36.

An Autonomous Institution

Accredited by NBA – AICTE and Accredited by NAAC – UGC with ‘A++’
Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

**COURSE CODE & NAME : 19CSB301 & AUTOMATA THEORY AND COMPILER
DESIGN**

III YEAR/ V SEMESTER

UNIT – I FINITE AUTOMATA AND REGULAR LANGUAGES

Topic: Central concepts of Automata Theory

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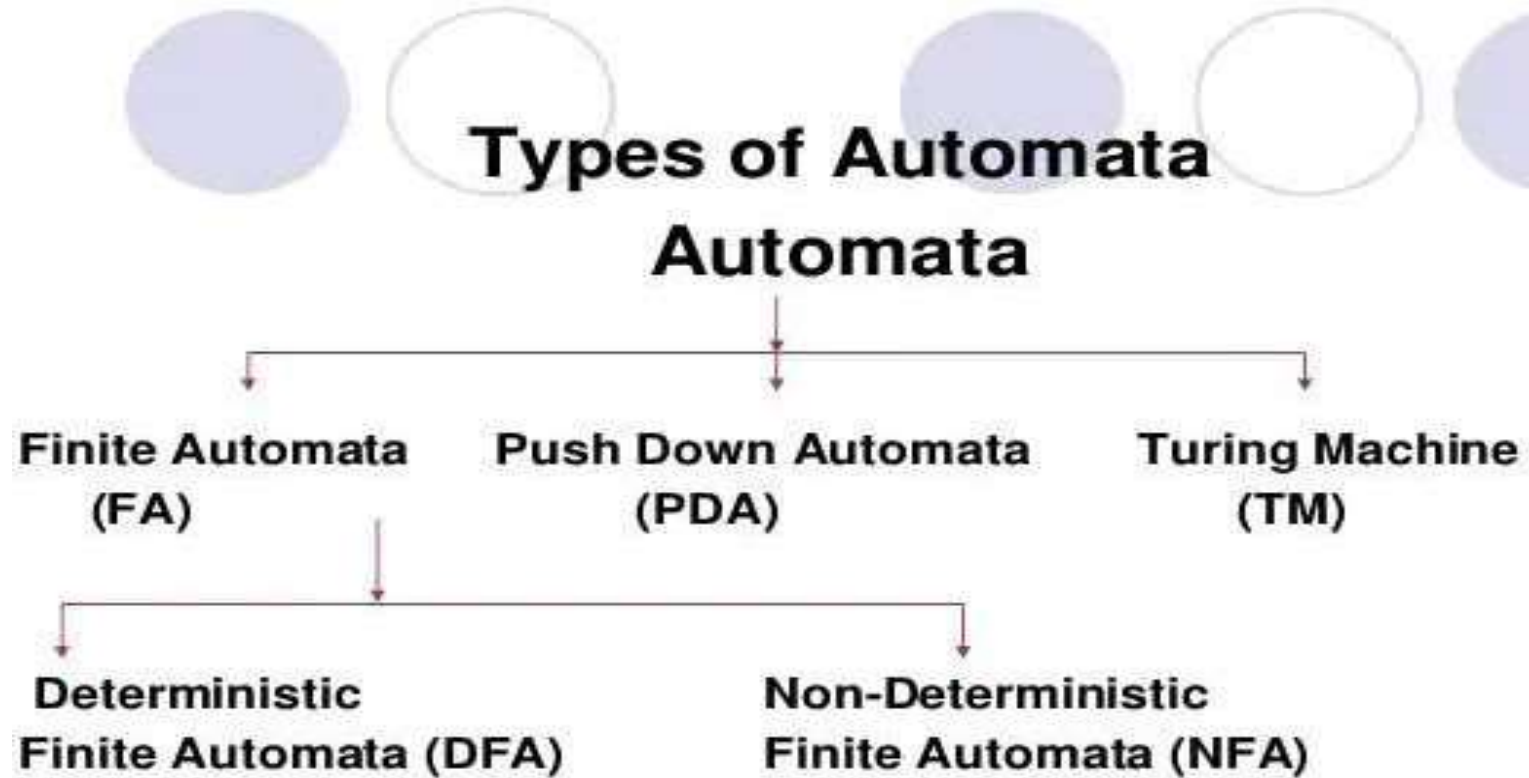


Introduction to Automata

- Theory of automata is a theoretical branch of computer science and mathematical.
- It is the study of abstract machines and the computation problems that can be solved using these machines.
- The abstract machine is called the automata.
- The main motivation behind developing the automata theory was to develop methods to describe and analyse the dynamic behaviour of discrete systems.
- This automaton consists of states and transitions. The **State** is represented by **circles**, and the **Transitions** is represented by **arrows**.
- Automata is the kind of machine which takes some string as input and this input goes through a finite number of states and may enter in the final state.



Types of Automata





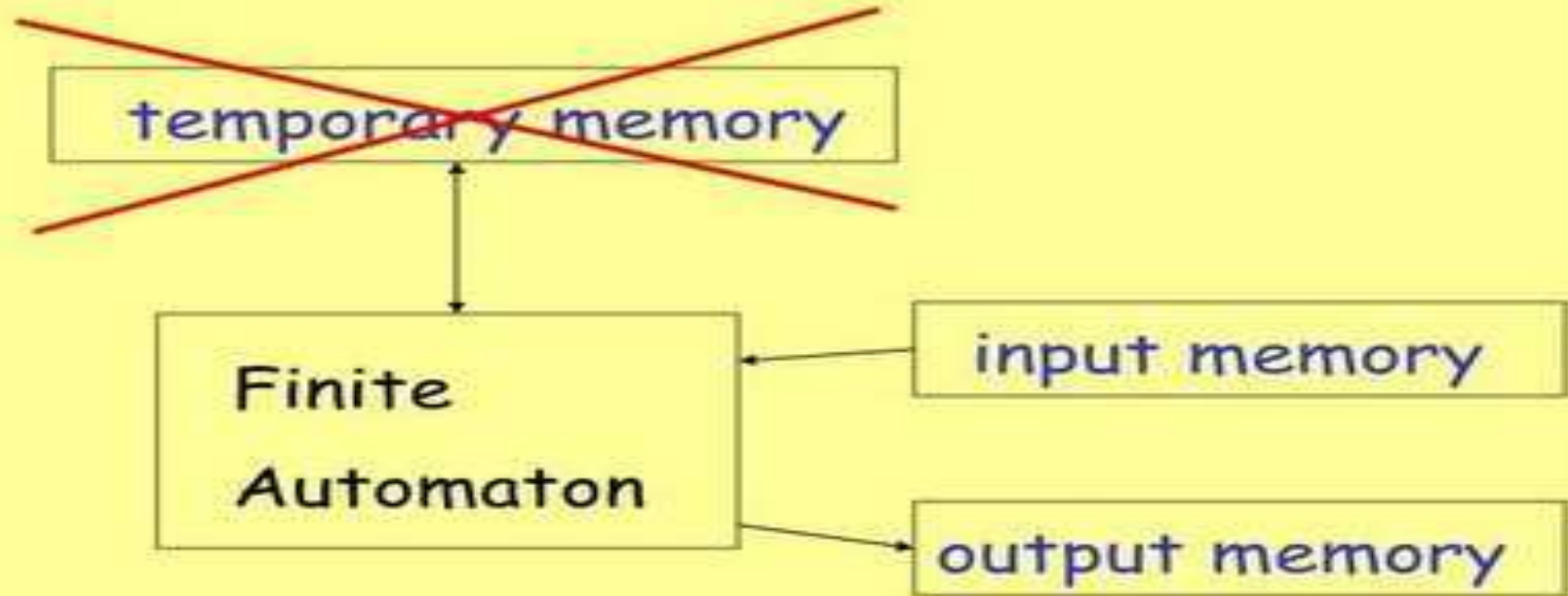
Types of Automata

Automata are distinguished by the temporary memory

- **Finite Automata:** no temporary memory
- **Pushdown Automata:** stack
- **Turing Machines:** random access memory



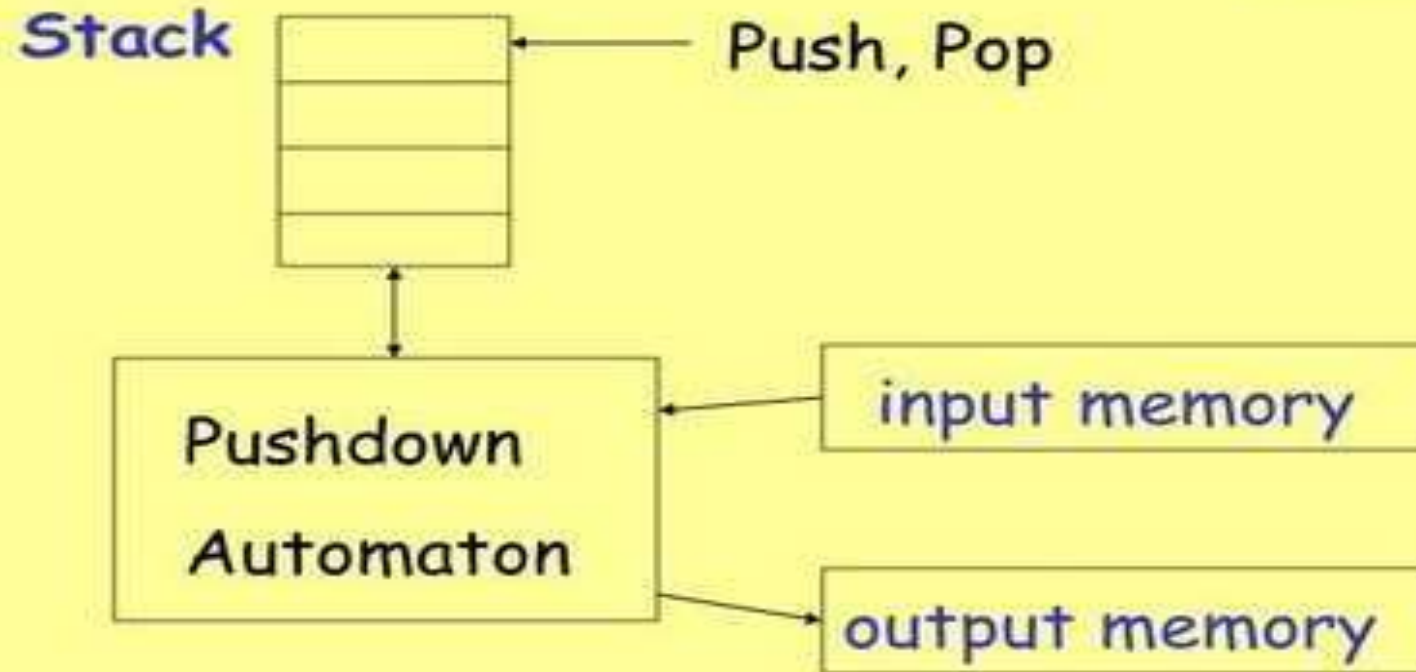
Types of Automata



Example: Vending Machines
(small computing power)



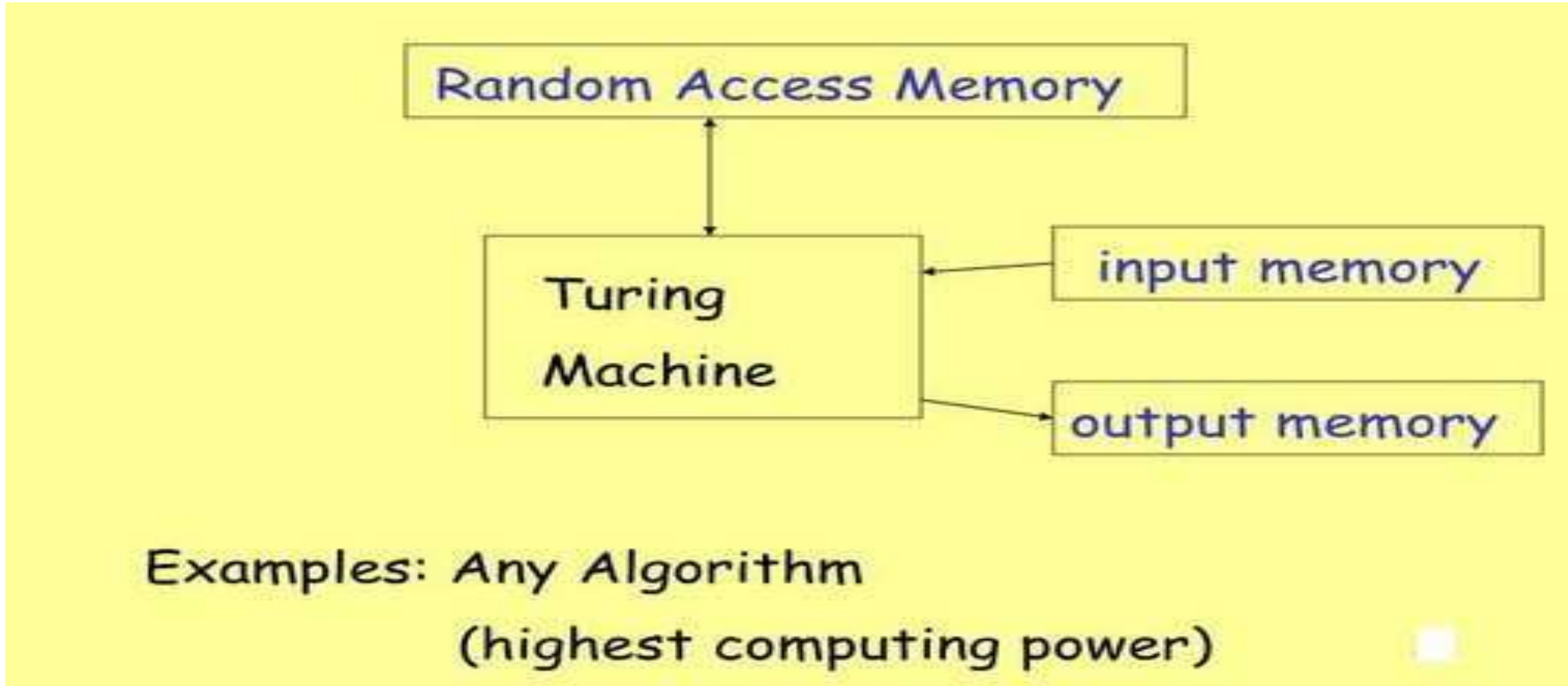
Types of Automata



Example: Compilers for Programming Languages
(medium computing power)

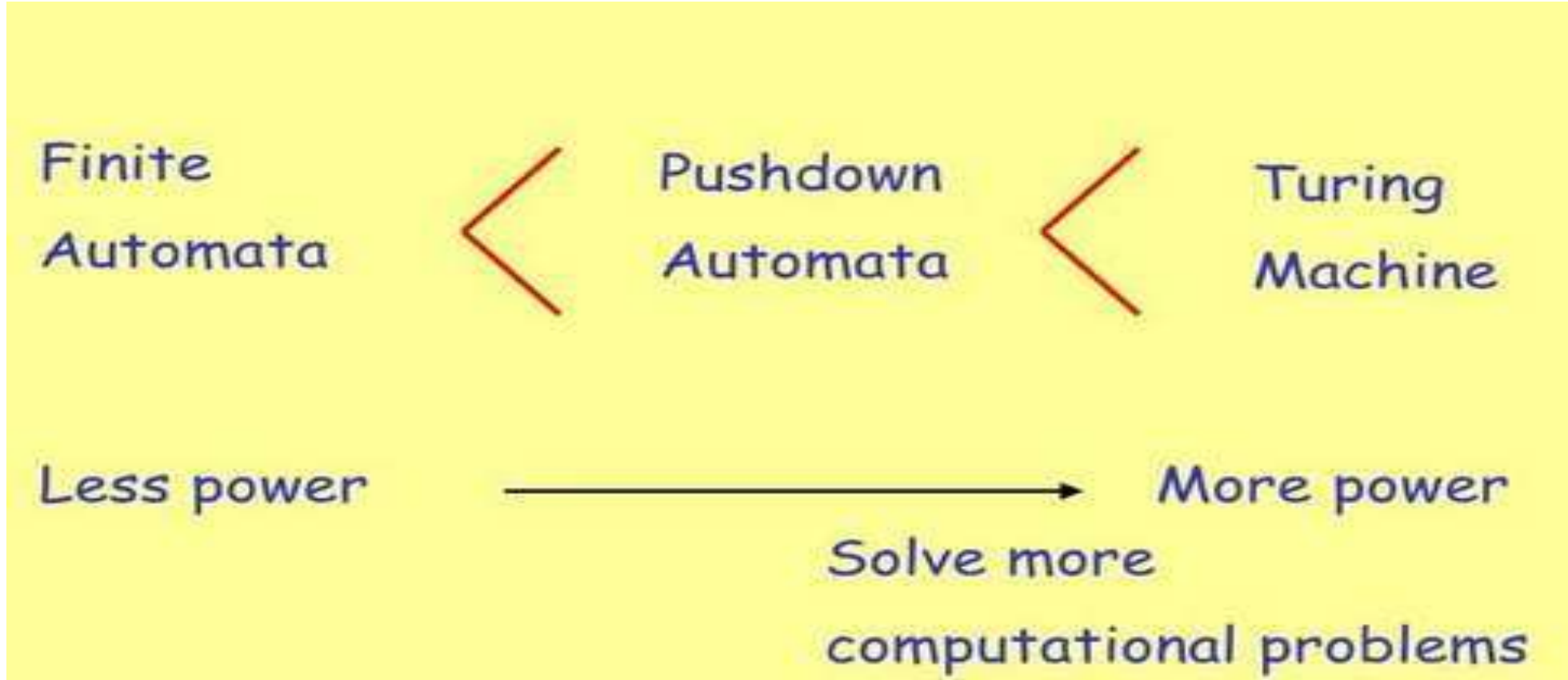


Types of Automata





Types of Automata





Types of Automata

Model	Language Recognition	Memory Management	Implementation
Finite Automata	Regular Languages	No temporary memory	Elevators, Vending Machines, Traffic Light, Neural Network (small computing power)
Pushdown Automata	Context-free Languages	Stack	Compilers for Programming Languages (medium computing power)
Turing machine	Unrestricted Grammar, Lambda Calculus (Computable Languages)	Random access memory	Any Algorithm (highest computing power)



Key Terminologies

Symbols:

Symbols are an entity or individual objects, which can be any letter, alphabet or any picture.

Example:

1, a, b, #

Alphabets:

Alphabets are a finite set of symbols. It is denoted by Σ .

Examples

$\Sigma = \{a, b\}$ $\Sigma = \{A, B, C, D\}$ $\Sigma = \{0, 1, 2\}$ $\Sigma = \{0, 1, \dots, 5\}$



Key Terminologies

String:

It is a finite collection of symbols from the alphabet. The string is denoted by w .

Example 1:

If $\Sigma = \{a, b\}$, various string that can be generated from Σ are $\{ab, aa, aaa, bb, bbb, ba, aba.....\}$.

A string with zero occurrences of symbols is known as an empty string. It is represented by ϵ .

The number of symbols in a string w is called the length of a string. It is denoted by $|w|$.



Key Terminologies

Language(Set of Strings with Rules)

A language is a collection of appropriate string. A language which is formed over Σ can be **Finite** or **Infinite**.

Example: 1

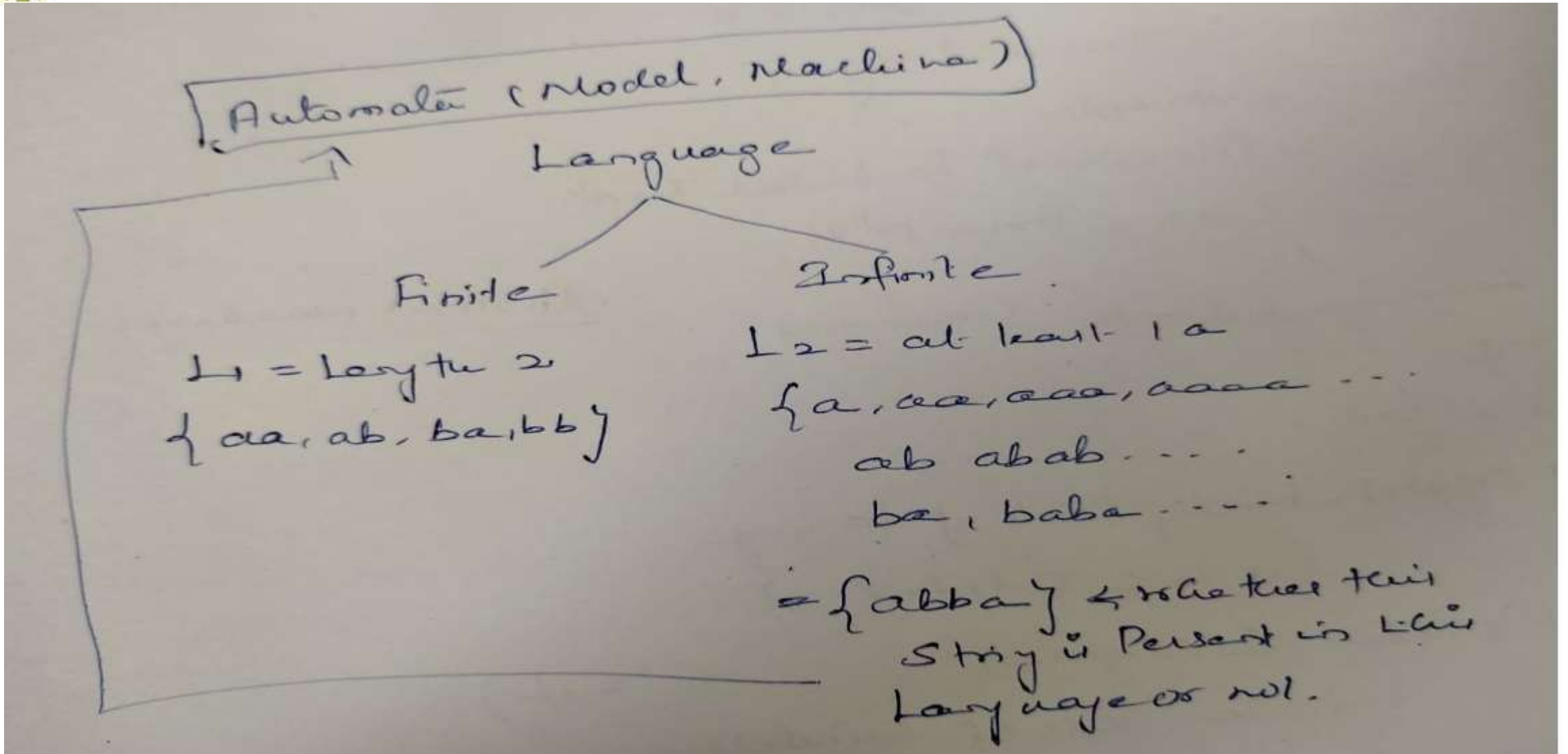
$L1 = \{\text{Set of string of length 2}\} = \{aa, bb, ba, bb\}$ **Finite Language**

Example: 2

$L2 = \{\text{Set of all strings starts with 'a'}\} = \{a, aa, aaa, abb, abbb, ababb\}$
Infinite Language



Key Terminologies





Key Terminologies

Empty String, Length of String, reverse of String, Power of alphabet, Power of String

$$\Sigma = \{a,b\} \quad \wedge \quad a \quad b \quad aa \quad ab$$

Empty String string that has no letter, also known as **Null string**, denoted by Λ , λ or ϵ
It's length is Zero (0)

Length of String is the number of letters in a string, denoted by $|s|$
Example: $s = abab \quad |s| = 4 \quad \text{or} \quad \text{length}(s) = 4 \quad \text{or} \quad \text{length}(abab) = 4$

Reverse of String Is obtained by writing letters of string in reverse order, denoted by $\text{Rev}(s)$ or $\overset{\curvearrowright}{S}$ Or $\text{Reverse}(s)$
Example: $s = abab \quad \text{Rev}(s) = baba \quad \text{Reverse}(s) = baba$

Power of Alphabet Determines that the strings made from alphabet will be of length equal to power of alphabet
 $\Sigma = \{a,b\}^2 \quad \{aa, ab, ba, bb\}$ Total number of letters in alphabet $\longrightarrow n^m \quad \overset{\text{Length/power}}{2^2 = 4}$

Power of string Determines the length of string
 $(bab)^2 = babbab$
 $ba^2b = baab$



Power of Alphabet

power set of Alphabet

i) Kleen plus

ii) Kleen closure

Kleen closure $\rightarrow \Sigma^*$

$$\begin{aligned}\Sigma^* &= \Sigma^0 \cup \Sigma^1 \cup \dots \cup \Sigma^n \\ &= \epsilon \cup \Sigma^1 \cup \Sigma^2 \cup \dots \cup \Sigma^n\end{aligned}$$

Kleen plus $\rightarrow \Sigma^+ = \Sigma^* - \epsilon$

$$\Sigma^+ = \Sigma^* - \epsilon = \Sigma \cup \Sigma^2 \cup \Sigma^3 \cup \dots \cup \Sigma^n$$



References

- John E. Hopcroft and Rajeev Motwani and Jeffrey D. Ullman, “Introduction to Automata Theory, Languages and Computation”, Second Edition, Pearson Education, New Delhi, (2007) (UNIT-I)
- Linz P. An introduction to formal languages and automata. Sixth edition, Jones and Bartlett Publishers; 2016.(UNIT-I)
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