



SNS COLLEGE OF TECHNOLOGY



Coimbatore-36.

An Autonomous Institution

Accredited by NBA – AICTE and Accredited by NAAC – UGC with ‘A++’
Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

**COURSE CODE & NAME : 19CSB301 & AUTOMATA THEORY AND COMPILER
DESIGN**

III YEAR/ V SEMESTER

UNIT – I FINITE AUTOMATA AND REGULAR LANGUAGES

Topic: Types of Grammar

Dr.B.Vinodhini

Associate Professor

Department of Computer Science and Engineering



Types of Grammar

- ***Grammar in Automata***

- **$G = (V, T, P, S)$**
- V – Non-Terminals / Variables / Auxillary Symbols (A,B,C,....)
 - Takes part in generation of sentence (Not a part of sentence)
- T – Terminals (small-case letters a,b,c,....)
- P – Production Rules
- S – Start Symbol

Example1

$V = \{S\}$

$T = \{a, b\}$

$P = \{S \rightarrow aSbS, S \rightarrow bSaS, S \rightarrow \epsilon\}$

$S = \{S\}$

Example2

$V = \{S, A, B\}$

$T = \{a, b\}$

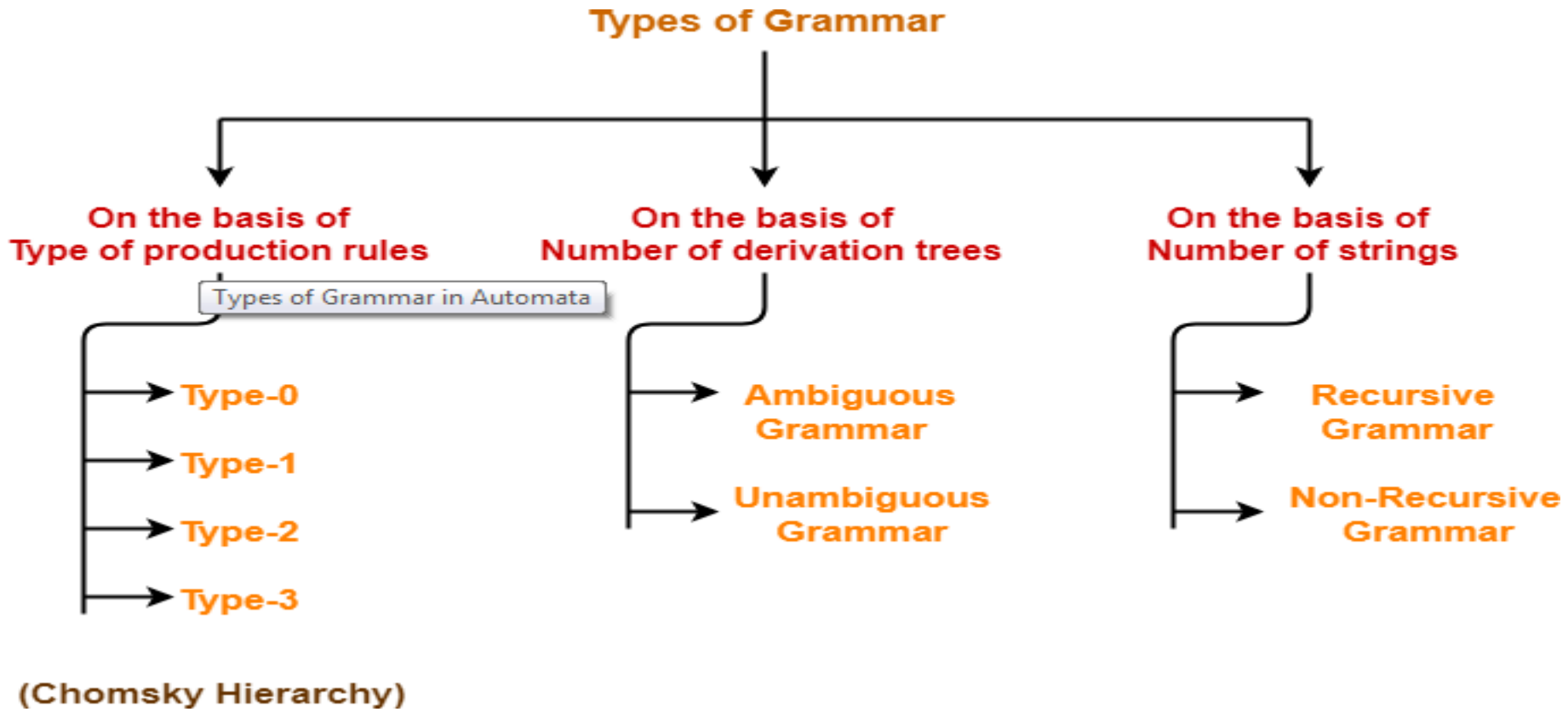
$P = \{S \rightarrow ABA, A \rightarrow BB, B \rightarrow ab, AA \rightarrow b\}$

$S = \{S\}$



Types of Grammar

T

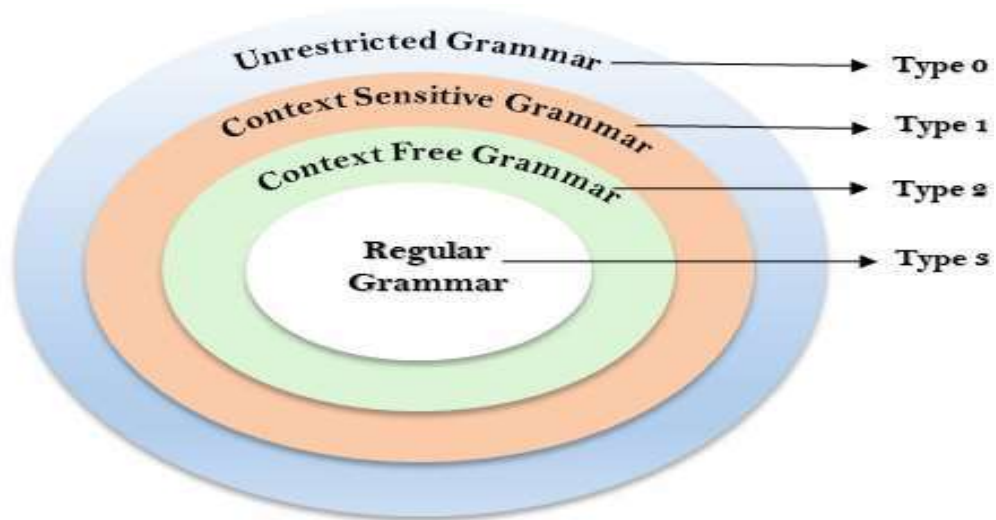




Chomsky Hierarchy



Grammar Type	Grammar Accepted	Language Accepted	Automaton
Type 0	Unrestricted grammar	Recursively enumerable language	Turing Machine
Type 1	Context-sensitive grammar	Context-sensitive language	Linear-bounded automaton
Type 2	Context-free grammar	Context-free language	Pushdown automaton
Type 3	Regular grammar	Regular language	Finite state automaton



Type 3 \subseteq Type 2, Type 1, Type 0
Type 2 \subseteq Type 1, Type 0
Type 1 \subseteq Type 0



Chomsky Hierarchy



- Type 0 (Unrestricted)

- $\alpha \rightarrow \beta$
- $\alpha \in (V+T)^+ \leftarrow$ excluding ϵ
- $\beta \in (V+T)^* \leftarrow$ including ϵ
- $\alpha \neq \epsilon$

- Type 1 (Context Sensitive Grammar)

- $\alpha \rightarrow \beta$
- $|\alpha| \leq |\beta|$

- Type 2 (Context Free Grammar)

- $\alpha \rightarrow \beta$
- $\alpha \in V$
- $\beta \in (V+T)^*$

- Type 3 (Restricted)

- $V \rightarrow VT^*/T^*$ (Right Regular Language) OR T^*V/T^* (Left Regular language)
- Example: $A \rightarrow aB$, $A \rightarrow a$



Chomsky Hierarchy



Rules

Type 0 $\rightarrow \alpha \neq \epsilon$

Type 1 $\rightarrow |\alpha| \leq |\beta|$

Type 2 $\rightarrow \alpha \in V, \beta \in (V+T)^*$

Type 3 $\rightarrow \alpha \rightarrow aB$ or $\alpha \rightarrow a$

Examples of type of Grammar

$\alpha \rightarrow \beta$

e 0 : $\alpha \neq \text{NULL}$
e 1 : $|\alpha| \leq |\beta|$
e 2 : $A \in V$
e 3 : $A \rightarrow aB$ or $A \rightarrow a$

2) $S \rightarrow Xa \checkmark$
 $X \rightarrow a \checkmark$
 $X \rightarrow aX \checkmark$
 $X \rightarrow abcX$
 $X \rightarrow \epsilon$

4.) $AB \rightarrow AbB$
 $A \rightarrow bcA$
 $B \rightarrow b$
 \downarrow
Type 1

3.) $X \rightarrow \epsilon \checkmark$
 $X \rightarrow a/aY \checkmark$
 $Y \rightarrow b \checkmark$
 \downarrow
Type 3

$S \rightarrow ACaB$
 $Bc \rightarrow acB$
 $CB \rightarrow DB$
 $aD \rightarrow Db$ \rightarrow **Type 1**

Type 2 \leftarrow



References

- John E. Hopcroft and Rajeev Motwani and Jeffrey D. Ullman, “Introduction to Automata Theory, Languages and Computation”, Second Edition, Pearson Education, New Delhi, (2007) (UNIT-I)
- Linz P. An introduction to formal languages and automata. Sixth edition, Jones and Bartlett Publishers; 2016.(UNIT-I)
- [Ramaiah k. Dasaradh](#) “Introduction to Automata and Compiler Design “ First Edition ,Prentice Hall India Learning Private Limited(2011)(UNIT-I to V)

