



Solution. Given : $\omega_{AP_1} = 10 \text{ rad/s}$; $\alpha_{AP_1} = 30 \text{ rad/s}^2$; $P_1A = 300 \text{ mm} = 0.3 \text{ m}$; $P_2B = AB = 360 \text{ mm} = 0.36 \text{ m}$

We know that the velocity of A with respect to P_1 or velocity of A ,

$$V_{AP_1} = V_A = \omega_{AP_1} \times P_1A = 10 \times 0.3 = 3 \text{ m/s}$$

Velocity of B and angular velocities of P_2B and AB

First of all, draw the space diagram, to some suitable scale, as shown in Figure (a). Now the velocity diagram, as shown in Figure (b), is drawn as discussed below:

1. Since P_1 and P_2 are fixed points, therefore these points lie at one place in velocity diagram.

Draw vector p_1a perpendicular to P_1A , to some suitable scale, to represent the velocity of A with respect to P_1 or velocity of A i.e. V_{AP_1} or V_A , such that

$$\text{vector } p_1a = V_{AP_1} = V_A = 3 \text{ m/s}$$

2. From point a , draw vector ab perpendicular to AB to represent velocity of B with respect to A (i.e. V_{BA}) and from point p_2 draw vector p_2b perpendicular to P_2B to represent the velocity of B with respect to P_2 or velocity of B i.e. V_{BP_2} or V_B . The vectors ab and p_2b intersect at b .

By measurement, we find that

$$V_{BP_2} = V_B = \text{vector } p_2b = 2.2 \text{ m/s} \text{ Answer.}$$

$$\text{and } v_{BA} = \text{vector } ab = 2.05 \text{ m/s}$$

We know that angular velocity of P_2B ,

$$\omega_{P_2B} = \frac{v_{BP_2}}{P_2B} = \frac{2.2}{0.36} = 6.1 \text{ rad/s (Clockwise) Ans.}$$

and angular velocity of AB ,

$$\omega_{AB} = \frac{v_{BA}}{AB} = \frac{2.05}{0.36} = 5.7 \text{ rad/s (Anticlockwise) Ans.}$$

**Acceleration of B and angular acceleration of P₂B and AB**

We know that tangential component of the acceleration of A with respect to P₁,

Radial component of the acceleration of A with respect to P₁,

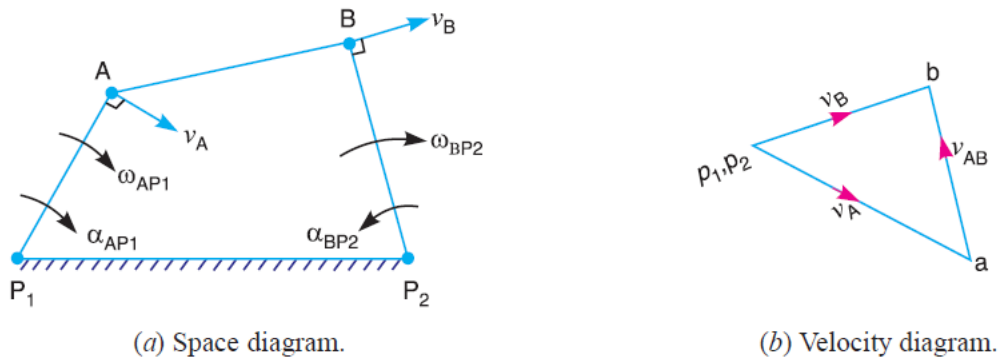
$$a_{AP_1}^r = \frac{v_{AP_1}^2}{P_1A} = \omega_{AP_1}^2 \times P_1A = 10^2 \times 0.3 = 30 \text{ m/s}^2$$

Radial component of the acceleration of B with respect to A.

$$a_{BA}^r = \frac{v_{BA}^2}{AB} = \frac{(2.05)^2}{0.36} = 11.67 \text{ m/s}^2$$

and radial component of the acceleration of B with respect to P₂,

$$a_{BP_2}^r = \frac{v_{BP_2}^2}{P_2B} = \frac{(2.2)^2}{0.36} = 13.44 \text{ m/s}^2$$



Figure

The acceleration diagram, as shown in Figure (c), is drawn as follows:

1. Since P₁ and P₂ are fixed points, therefore these points will lie at one place, in the acceleration diagram. Draw vector $p_1'x$ parallel to P₁A, to some suitable scale, to represent the radial component of the acceleration of A with respect to P₁, such that

$$\text{vector } p_1'x = a_{AP_1}^r = 30 \text{ m/s}^2$$

2. From point x, draw vector xa' perpendicular to P₁A to represent the tangential component of the acceleration of A with respect to P₁, such that

$$\text{vector } xa' = a_{AP_1}^t = 9 \text{ m/s}^2$$