



(An Autonomous Institution) Coimbatore – 35

### **DEPARTMENT OF MATHEMATICS**

**UNIT - II - COMBINATORICS** 

# THE PRINCIPLE OF INCLUSION - EXCLUSION:

n (AUB) = n (A) +n(B) - n (ANB) (01) | AUB| = |A|+|B|- |ANB| |AUBUC| = |A| + |B| + |C| - |A nB| - |Anc| - |Bnc| + [An Bnc] [AUBUCUD] = [A]+ [B]+ [C]+[D] - [ANB] - [ANB] - [AND]-|Bnc|-IBnd|-|Cnd|+|AnBnc|+ IAMBADI + | BACADI + |AMCADI-|ANBOCOD|

D In a survey of 100 students, it was found that 30 students mathematics, 54 studied statuties, or studied operation Research, I studied all The three subjects. 20 studied mathematics and statistics, 3 studied mathematics and operations research and is studied statistics and (i) How many students studied none of there subjects? Operations Research

(ii) How many Studente Studied only mathematics ?

soln! Let A denote the students who studied mathematics Let B denote the students who studied statistics Let a denote the objections who studied OR.

Then IAI = 30 ; IBI = 54; ICI = 25 |Ans| = 20; |Anc| = 3; |Bnc| = 15 IANBACI=1





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(i) No. of students studied none of these subjects =100-|AUBUC|

... By principle of Inclusion - Enclusion,

|AUBUC|= |A|+|B|+|C|-|A|B|-|A|C|-|B|C|+|A|B|C|

= 30+54+25-20-3-15+1

= 72

... No. of students studied none of these = 100-72

Subjects = 28

(2) How many positive integers not exceeding 1000 are olinsible by 7 or 11?

Let A denote The set of the integers not exceeding 1000 that are divisible by 7.

Let B denote The set of the integers not exceeding 1000 that are divisible by 11.

Then  $|A| = \left[\frac{1000}{7}\right] = \left[142.8\right] = 142$ .  $|B| = \left[\frac{1000}{7}\right] = \left[90.9\right] = 90$ 





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$$|A \cap B| = \left[\frac{1000}{7 \times 11}\right] = \left[12.97 = 12.$$

No. 9 +ve integer not exceeding 11

... No. 9 +ve integer not exceeding 1000 that are divisible by either 7 of 11 is IAUB)

3) Find the no. of integers between I to 250 that are not divisible by any of the integers 4,3,5 &7.

$$|B| = \left[\frac{9m}{3}\right] = 83$$

Now, the no. of integer bottom 1. to 250? = IANB! = [250] that are divisible by 283





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