



SNS COLLEGE OF TECHNOLOGY

Coimbatore-35
An Autonomous Institution



Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A+' Grade
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

23ECB221 – DIGITAL ELECTRONICS

II YEAR/ III SEMESTER

UNIT 1 – MINIMIZATION TECHNIQUES AND LOGIC GATES

TOPIC - KARNAUGH MAP MINIMIZATION ,DON'T CARE CONDITIONS- Problems



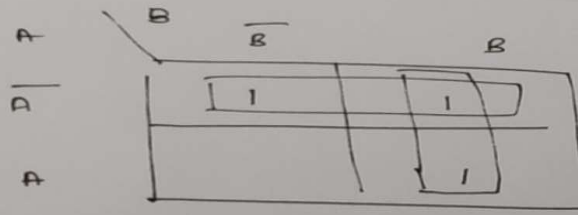
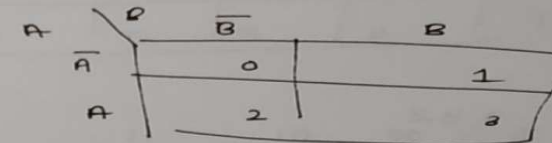
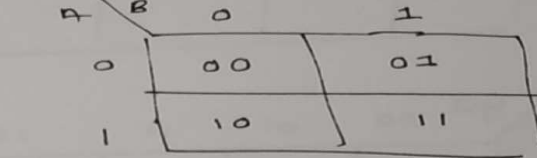
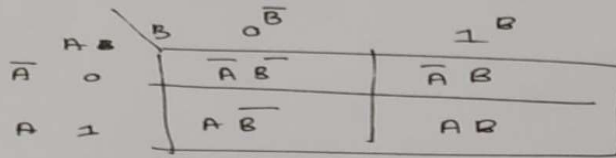
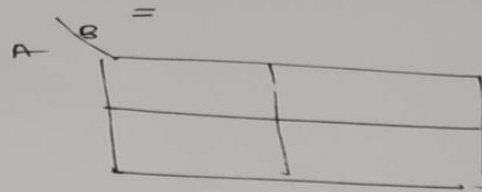
Two variable k-map

$$F = \bar{A}\bar{B} + \bar{A}B + AB$$

n = number of variables

$$n = 2$$

$$\text{no of columns in k-map} = 2^n = 2^2 = 4$$



$$F = \bar{A} + B$$



Three variable k-map.

$$F(x, y, z) = \sum (2, 3, 4, 5)$$

$$n = 3$$

$$\text{No. of columns} = 2^2 = 4$$

| x \ yz | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0 | | | | |
| 1 | | | | |

| x \ yz | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0 | 0 | 1 | 2 | 3 |
| 1 | 4 | 5 | 6 | 7 |

| x \ yz | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0 | | | 1 | 1 |
| 1 | 1 | 1 | | |

Annotations: $\overline{x}y$ (pointing to the top-right group of 1s) and $x\overline{y}$ (pointing to the bottom-left group of 1s).

so

$$f(x, y, z) = \sum (2, 3, 4, 5) = \overline{x}y + x\overline{y}$$



3. Minimize the following standard pos expression using k-map.

$$Y = \Pi M(0, 2, 3, 5, 7)$$

Sol:-
 $n = 3, 2^3 = 8$

| x | yz | 00 | 01 | 11 | 10 |
|---|----|----|----|----|----|
| 0 | | 0 | 1 | 3 | 2 |
| 1 | | 4 | 5 | 7 | 6 |

| x | yz | 00 | 01 | 11 | 10 |
|---|----|----|----|----|----|
| 0 | | 0 | | 0 | 0 |
| 1 | | | 0 | 0 | |

Group 1

| x | yz | yz | y \bar{z} | $\bar{y}z$ | $\bar{y}\bar{z}$ |
|---|----|----|-------------|------------|------------------|
| 0 | | 0 | | 0 | 0 |
| 1 | | | 0 | 0 | |

Group 2

| x | yz | yz | y \bar{z} | $\bar{y}z$ | $\bar{y}\bar{z}$ |
|---|----|----|-------------|------------|------------------|
| 0 | | 0 | | 0 | 0 |
| 1 | | | 0 | 0 | |

Group 3

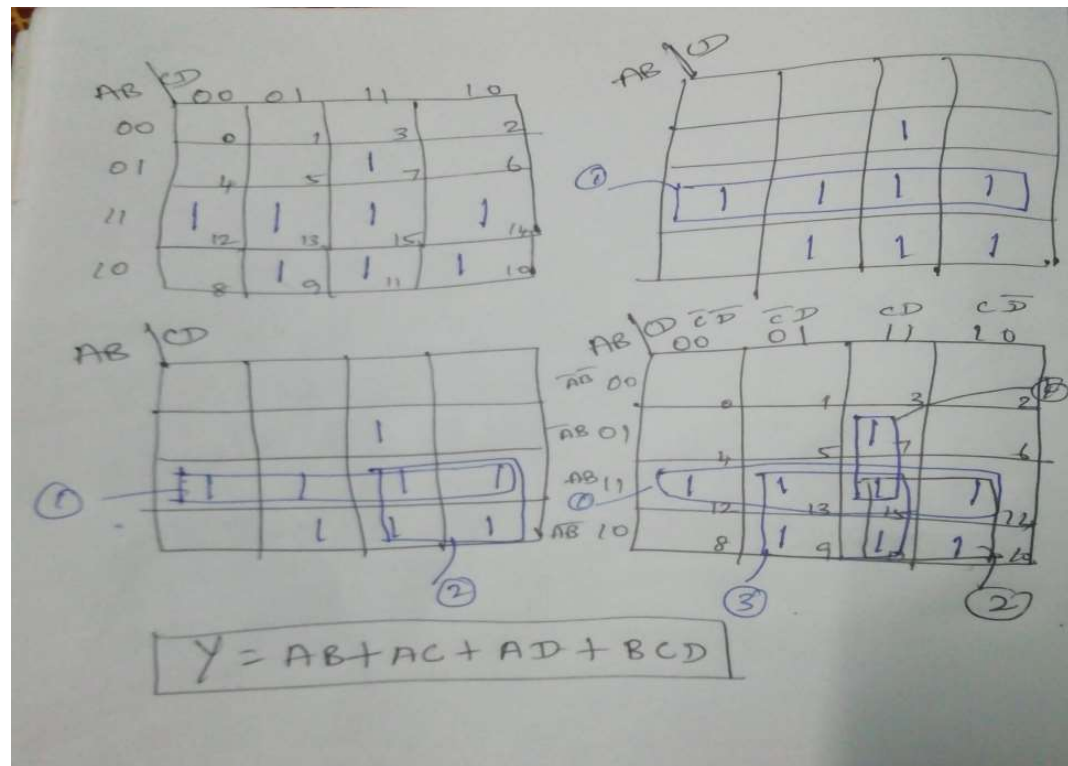
$$Y = (x + z) \cdot (\bar{y} + \bar{z}) \cdot (\bar{x} + \bar{z})$$



KARNAUGH MAP



4. Simplify the expression $Y = \sum m(7, 9, 10, 11, 12, 13, 14, 15)$, using the K-map method.

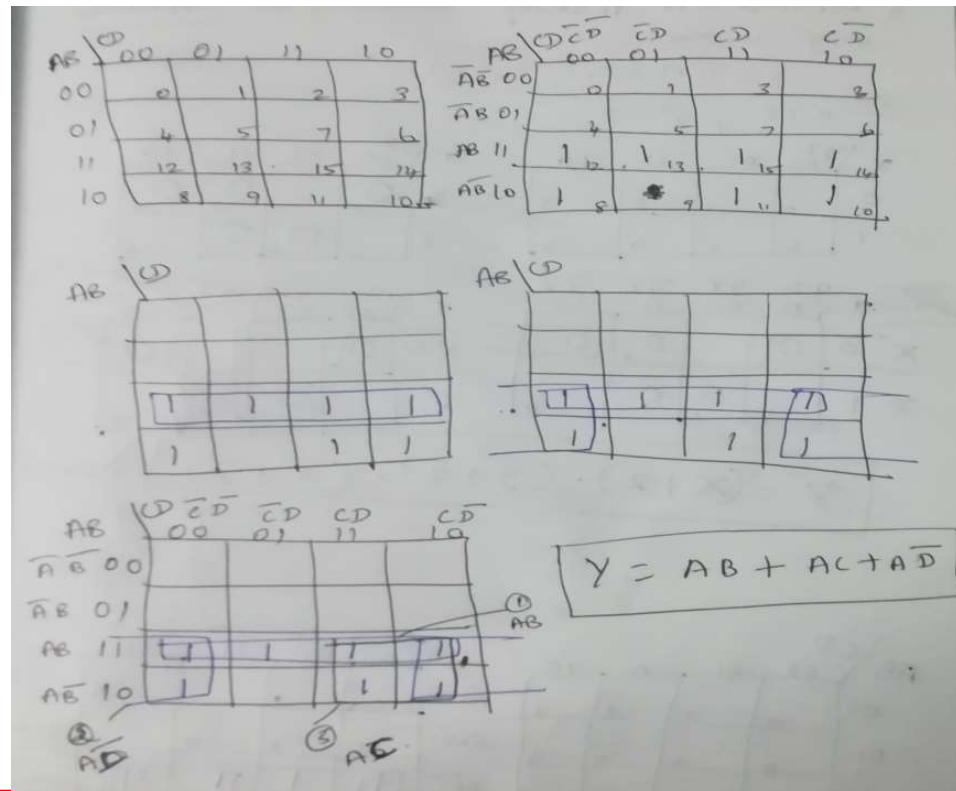




KARNAUGH MAP - Simplifications



5. Plot the logical expression $ABCD + AB'C'D' + AB'C + AB$ on a 4 variable K- map and obtain the simplified expression from the K- map.





Don't Care Conditions

- Don't Care conditions allow us to replace the empty cell of a K-Map to form a grouping of the variables.
- While forming groups of cells, we can consider a “Don't Care” cell as either 1 or 0 or we can simply ignore that cell.
- Don't Care condition can help us to form a larger group of cells.



Don't Care Conditions



Don't Care Conditions:-
It is represented as 'X' may be assumed to be 0 or 1 as per the requirement for simplification.

Problem:-
Simplify the Boolean expression using K-map.

$$Y = \sum m(1, 3, 7, 11, 15) + d(0, 2, 5)$$

|
minterms

↳ don't care

| CD \ AB | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | X | 1 | 1 | X |
| 01 | 4 | X | 5 | 7 |
| 11 | 12 | 13 | 1 | 14 |
| 10 | 8 | 9 | 1 | 15 |

don't care treated as 1

simplified expression is,

$$Y = CD + \overline{A}B$$



THANK YOU