



# SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)

Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai

Accredited by NAAC-UGC with 'A++' Grade (Cycle III) &

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COIMBATORE-641 035, TAMIL NADU

DEPARTMENT OF MATHEMATICS

23MAT101 – MATRICES AND CALCULUS

UNIT III – DIFFERENTIAL CALCULUS

PART A QUESTIONS

1. Find the curvature of the curve  $2x^2 + 2y^2 + 5x - 2y + 1 = 0$ .
2. Find the radius of curvature at  $(x, y)$  for the curve  $a^2y = x^3 - a^3$ .
3. Find  $\rho$  for the curve  $y = c \log \sec \left( \frac{x}{c} \right)$  at any point  $(x, y)$ .
4. Find the radius of curvature of the curve  $y = \log \sin x$  at  $x = \frac{\pi}{2}$ .
5. If  $y = x + 3x^2 - x^3$ , find  $\rho$  at  $x = 0$ .
6. Write the formula for centre of curvature and the equation of the circle of curvature.
7. Find the radius of curvature at  $\left(1, \frac{3}{2}\right)$  on the curve  $2y = x(1 - x + x^2)$ .
8. Find the radius of curvature at  $(c, c)$  on the curve  $y = c^2$ .
9. Find the envelope of family of straight lines  $mx + \frac{c}{m}$ ,  $m$  being the parameter.
10. Find the envelope of  $y = mx + \sqrt{a^2m^2 + b^2}$  where  $m$  is a parameter.
11. Find the envelope of  $\frac{x \cos \theta}{a} + \frac{y \sin \theta}{b} = 1$ , ' $\theta$ ' being the parameter.
12. For the curve  $x^2 = 2c(y - c)$  find the radius of curvature at  $(0, c)$ .
13. Find the envelope of  $(x - a)^2 + (y - a)^2 = 2a$ ,  $a$  being the parameter.
14. Find the points on the parabola,  $y^2 = 4x$  at which radius of curvature is  $4\sqrt{2}$ .
15. Give the radius of curvature of the curve given by  $x = 3 + 2 \cos \theta$ ,  $y = 4 + 2 \sin \theta$ .