



HEXAGONAL CLOSED PACKED STRUCTURE



• It consists of three layers of atoms.

• The bottom layer has six corner atoms and one face centred atom.

• The middle layer has three full atoms.

• The upper layer has six corner atoms and one face centred atom.

- Each and every corner atom contributes 1/6 of its part to one unit cell.
- The number of total atoms contributed by the corner atoms of both top and bottom layers is $1/6 \times 12 = 2$.

• The face centred atom contributes 1/2 of its part to one unit cell.

• Since there are 2 face centred atoms, one in the top and the other in the bottom layers, the number of atoms contributed by face centred atoms is $1/2 \times 2 = 1$.

• Besides these atoms, there are 3 full atoms in the middle layer.

• Total number of atoms present in an HCP unit cell is 2+1+3 = 6.

CO-ORDINATION NUMBER (CN)

- The face centered atom touches 6 corner atoms in its plane.
- The middle layer has 3 atoms.





- There are three more atoms, which are in the middle layer of the unit cell.
- Therefore the total number of nearest neighbours is 6+3+3=12.

ATOMIC RADIUS (R)

- Consider any two corner atoms.
- Each and every corner atom touches each other. Therefore a = 2r.
- i.e., The atomic radius, r = a/2

ATOMIC PACKING FACTOR (APF)

APF = v/Vv = 6 × 4/3 πr³ Substitute r = a/2

$$v = 6 \times 4/3 \pi \frac{a^3}{8}$$

$$v = \pi a^3$$



AB = AC = BO = `a`. CX = c/2 where $c \rightarrow$ height of the hcp unit cell.

Area of the base = $6 \times$ area of the triangle ABO = $6 \times 1/2 \times AB \times OO'$ Area of the base = $6 \times 1/2 \times a \times OO'$ In triangle O'OP

In triangle O'OB $\frac{O'OB}{OB} = 30^{\circ}$ $\frac{OO'}{BO} = \frac{OO'}{a}$

 \therefore OO' = a cos 30° = a $\sqrt{\frac{3}{2}}$ Now, substituting the value of OO',

 $\sqrt{\frac{3}{2}}$





Area of the base = $6 \times 1/2 \times a \times$ V = Area of the base × height

$$V = \frac{3\sqrt{3}a^2}{2} \times c$$

$$\therefore APF = \frac{V}{V} = \frac{\pi a^3}{\frac{3\sqrt{3} a^2 c}{2}}$$

$$\therefore APF = \frac{2\pi a^3}{3\sqrt{3}a^2c} = \frac{2\pi}{3\sqrt{3}} \frac{a}{c}$$

Determination of c/a ratio:

In the triangle ABA', **Cos 30°** = |A'AB|= 30°





$$\therefore AA' = AB \cos 30^{\circ} = a\sqrt{3/2}$$

But $AX = 2/3 AA' = 3^{2} - a \frac{3\sqrt{2}}{2}$
i.e. $AX = \sqrt{3}$
In the triangle
 $AXC, AC^{2} = AX^{2}$
 $+ CX^{2}$
Substituting the values of AC, AX and CX,

$$a^{2} = \left(\frac{a}{\sqrt{3}}\right)^{2} + \left(\frac{c}{2}\right)^{2}$$

$$a^{2} = \frac{a^{2}}{3} + \frac{c^{2}}{4}$$

$$\frac{c^{2}}{4} = a^{2} - \frac{a^{2}}{3}$$

$$\frac{c^{2}}{4} = a^{2} \left(1 - \frac{1}{3}\right)$$

$$\frac{c^{2}}{a^{2}} = \frac{8}{3}$$

$$\frac{c}{a} = \sqrt{\frac{8}{3}}$$

Now substituting the value of c/a to calculate APF of an hcp unit cell,

$$APF = \frac{2\pi}{3\sqrt{3}} \sqrt{\frac{3}{8}}$$
$$= \frac{2\pi}{3\sqrt{3}} \frac{\sqrt{3}}{2\sqrt{2}}$$
$$\pi$$

Mr.D.: \therefore APF = $\frac{\pi}{3\sqrt{2}}$ = 0.74 Department of Physics/SNSCT



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