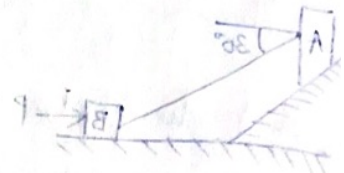
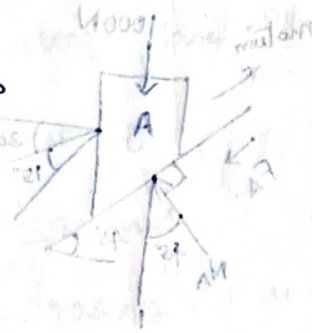
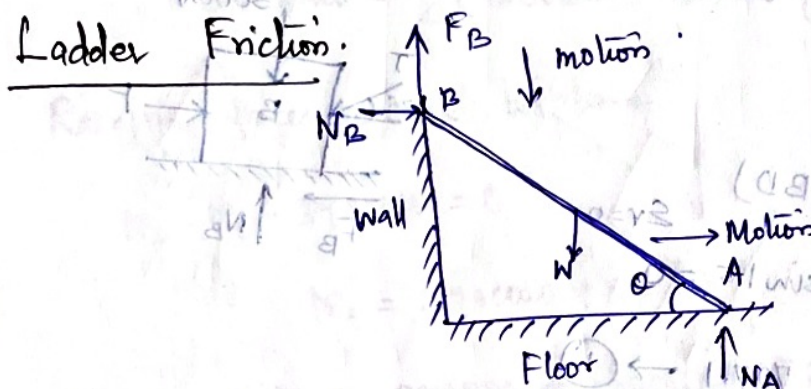


Simple Contact Friction:

- ① Ladder Friction
- ② Wedge "
- ③ Screw "
- ④ Belt "



Ladder Friction:



Ladder length = l

$\theta \Rightarrow$ angle of friction

Frictional force at B, F_B will act upwards

$$M_B = \frac{F_B}{N_B} \quad \text{or} \quad F_B = M_B N_B$$

$$M_A = \frac{F_A}{N_A}$$

For impending motion of ladder, the equilibrium eqn $\sum H = 0$ and $\sum M = 0$ and $F = \mu N$.

① A uniform ladder of weight 1000 N and of length 4 m rests on a horizontal ground and leans against a smooth vertical wall. The ladder makes an angle of 60° with horizontal. When a man of weight 750 N stands on ladder at a distance 3 m from the top of the ladder, the ladder is at the point of sliding. Determine the coefficient of friction between the ladder and the floor.

$$F_A = \text{Friction force at A} = \mu_A N_A$$

$$F_B = 0 \text{ (due to smooth wall)}$$

$$\mu_A = \text{coefficient of friction at A}$$

$$N_A, N_B = \text{Normal reactions at A, B.}$$

$$\text{Self weight, } W = 10000 \text{ N}$$

$$\text{Weight of man} = 750 \text{ N}$$

$$\text{Applying } \sum V = 0 \text{ (}\uparrow\text{)}$$

$$N_A - 10000 - 750 = 0$$

$$\underline{N_A = 1750 \text{ N}}$$

$$\sum H = 0 \text{ (}\rightarrow\text{)}$$

$$N_B - F_A = 0$$

$$N_B - \mu_A N_A = 0$$

$$N_B = \mu_A \times 1750 \rightarrow \textcircled{1}$$

$$\sum M_A = 0 \text{ (}\curvearrowright\text{)} \Rightarrow \text{Taking moment of all forces about A}$$

$$(N_B \times BG) - (10000 \times AF) - (750 \times AE) = 0$$

$$BG = 4 \sin 60 = 3.464 \text{ m}$$

$$AE = 1 \cos 60 = 0.5 \text{ m}$$

$$(N_B \times 3.464) - (10000 \times 1) - (750 \times 0.5) = 0$$

$$N_B = 396.9 \text{ N}$$

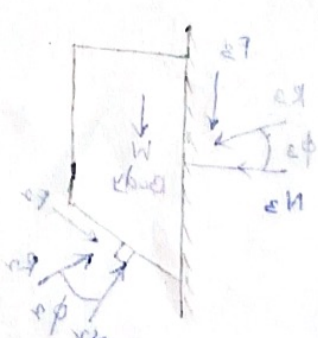
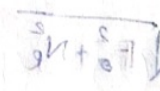
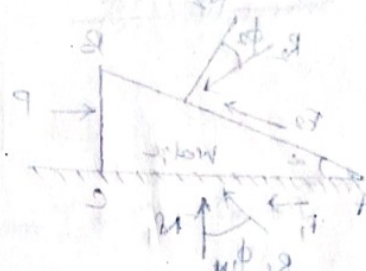
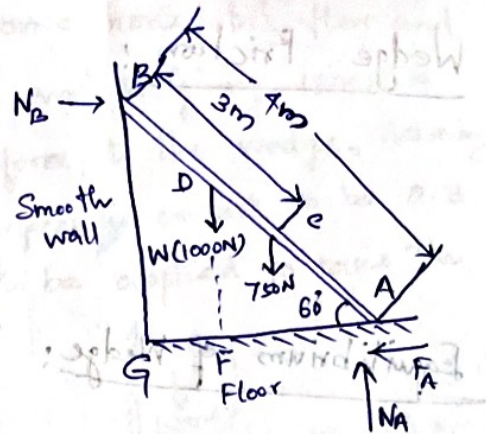
$$\boxed{N_B = 396.9 \text{ N}}$$

$$\text{sub } N_B \text{ in } \textcircled{1}$$

$$N_B = \mu_A \times 1750$$

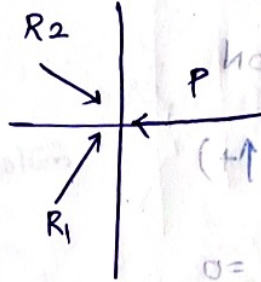
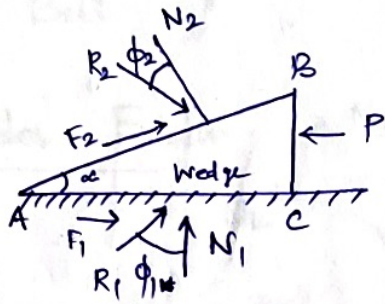
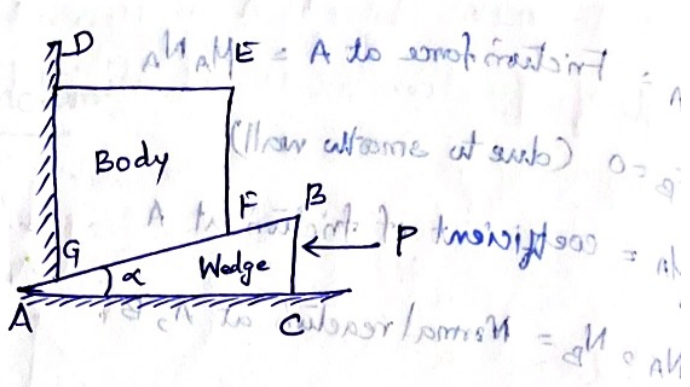
$$\mu_A = \frac{N_B}{1750} = \frac{396.9}{1750} = 0.226$$

$$\text{Coefficient of friction b/w ladder \& floor} = 0.226$$



Wedge Friction:

Equilibrium of Wedge:



$$F_2 = \mu_2 N_2 \quad F_1 = \mu_1 N_1$$

single Resultant $R = \sqrt{F_1^2 + N_1^2}$

R_1 and R_2 are drawn on wedges

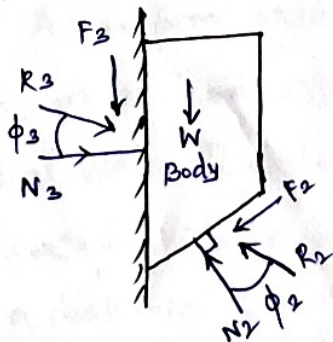
$$R_1 = \sqrt{F_1^2 + N_1^2} \quad R_2 = \sqrt{F_2^2 + N_2^2}$$

F_1 and $F_2 \rightarrow$ limiting friction
 R_1 and R_2 makes the angles ϕ_1 and ϕ_2 called angle of friction

with line of action of respective normal reactions N_1 and N_2 .

$R_1, R_2, P \rightarrow$ coplanar concurrent forces in equilibrium.

Equilibrium of body



R_2, R_3 and self weight w are coplanar concurrent forces in equilibrium.

$$\sum F_x = 0 \quad \sum F_y = 0$$

coefficient of friction $\mu = \frac{F}{N}$