



UNIT 5 Z - Transforms and Difference equations
Formation of Difference Equations

Difference Equations

A difference equation is a relation between the differences of an unknown function at one or more general values of the argument.

Formation of difference Equations:

1. Form the difference equation from

i) $y_n = a + b3^n$

ii) $y_n = A2^n + Bn$

Soln

b) $y_n = a + b3^n \rightarrow \textcircled{1}$

$y_{n+1} = a + b3^{n+1}$
 $= a + b3^n \cdot 3 \rightarrow \textcircled{2}$

$y_{n+2} = a + b3^{n+2}$
 $= a + b3^n \cdot 9 \rightarrow \textcircled{3}$

$y_n = A3^n$
 $y_{n+1} = A3^{n+1} = A3^n \cdot 3$
 $= A3^n + A3^n$
 $y_{n+2} = A3^{n+2}$
 $\begin{vmatrix} y_n & 1 \\ y_{n+1} & 3 \end{vmatrix}$
 $3y_n - y_{n+1} = 0$

Eliminating from $\textcircled{1}$, $\textcircled{2}$ and $\textcircled{3}$.

$$\begin{vmatrix} y_n & 1 & 1 \\ y_{n+1} & 1 & 3 \\ y_{n+2} & 1 & 9 \end{vmatrix} = 0$$

$y_n(9-3) - 1(9y_{n+1} - 3y_{n+2}) + (y_{n+1} - y_{n+2}) = 0$

$6y_n - 8y_{n+1} + 2y_{n+2} = 0 \quad (\div 2)$

$3y_n - 4y_{n+1} + y_{n+2} = 0$