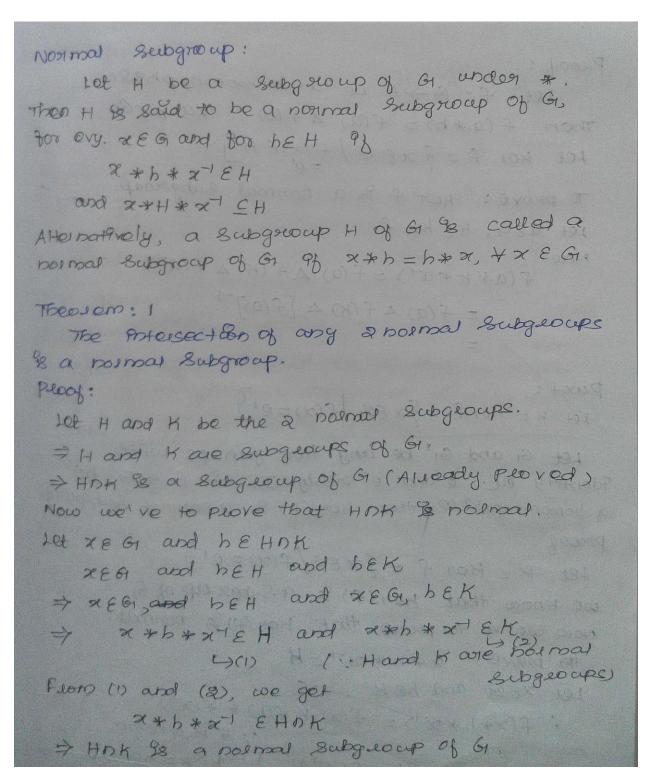




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Theorem 2: Let G and G' be any two groups with Alt G and G' be any two groups with Adentity et: e and e' nesty. If f: G > G' be a homomorphism, then how (f) is a normal subspicup.
periods: Let $K = Kor f = \frac{2}{2} \times \frac{6}{5} f(x) = e^{\frac{1}{3}}$ we know that $Kor(f)$ is a subgroup of G Now we've to prove that $Kor(f)$ is normal.
TO prove $x*h*x^{-1}E^{n}$ Let $x \in G$ and $h \in K$ $f(x*h*x^{-1}) = f(x) + f(h) + f(x^{-1})$ $f(x*h*x^{-1}) = f(x) + f(h) + f(x^{-1})$
$= f(x) * e' * f(x^{-1}) \qquad [::hek=keef]$ $= f(x) * f(x^{-1})$
$= f(e)$ $= e'$ $f(x*b*x^{-1}) = e'$ $= p x*h * x^{-1} \in \mathbb{N}$
i. K=Kelf & a polmal subgroup of G.





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Theoriem: 3 Fundamental Theorem of
                   Hemomosph9300
 Every homomosphic amage of a group G
  Bomosphac to some quotherst governo of G.
98
          (02)
  Let f: G1 -> G1 be a onto bondonouphism
of groups with keened to then G/x = G1.
Peoof:
 Let f: G > G' be a homomorphism
  Let it be the teener of the home.
 clearly & Bs a normal subgroup of G.
TO PLOYE GIK SE SEOMOLPHOC GIK ~ GI
i). To prove of & well defended.
  Lot b: G/K -> G' by o(K*a) = f(a)
 Consador.
           おおのこかおり
             => axb EK
             >> f(a*b)=e'
           f(a) * f(b') = e'
           f(a) * [f(b)] = e1
            f(a) * [f(b)] * f(b) = e' * f(b)
               +(a) * e = e * +(b)
                     f(a) = f(b)
                $ (K*a) = $ (K*b)
              : o is well defined
 ii). To Plove + & 1-1.
   re, $(K*a) = $(K*b) = K*a = K*b
   consider \phi(\kappa*a) = \phi(\kappa*b)
```





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```
f(a) = f(b)
   f(a) * f(b') = f(b) * f(b')
      f(a*b") = f(b*b")
            = f(e)
       > a* b & EK
        K*a= K*B
        ·· $ 18 1-1.
Iii) To peove & B onto.
     Let begi
 Bance f le onto. J an elt. a & Gr Such that
f(a) = b.
  \Rightarrow f(a) = \phi (k*a) = b
       iv). To playe of is a home,
Noco,
    $(K*a* K*b) = $(K*9*b)
     = f(a*b)
      = f(a) * f(b)
      = 0(149) + 6(146)
     ob a borno.
  2900 p & 1-1 & onto, homo.
   · + is an 920marph9 &m b/co 61/4 and G1
     ⇒ GIK ~ GI.
```