

Quartile deviation:

Quartile deviation (Q.D) is an absolute measure of dispersion and it is based upon upper quartile (Q_3) and lower quartile (Q_1). It represents the average difference between two quartiles and is given by

$$Q.D = \frac{Q_3 - Q_1}{2}$$

where, $Q_3 - Q_1$ is called Inter quartile. So Q.D is called as Semi Inter quartile range.

The relative measure of Q.D is called Coefficient of Q.D.

$$\text{Coefficient of } Q.D = \frac{Q_3 - Q_1}{Q_3 + Q_1}$$

Example: 1

From the following data calculate quartile deviation and its coefficient.

1490 692 777 335 582 488 753 384

407 672 522

Solution: Arrange it in ascending order

335 384 407 488 522 582 672 692

753 777 1490



$$\begin{aligned}Q_1 &= \text{Size of } \left[\frac{n+1}{4} \right]^{\text{th}} \text{ item} \\&= \text{Size of } \left[\frac{11+1}{4} \right]^{\text{th}} \text{ item} \\&= \text{Size of } \left[\frac{12}{4} \right]^{\text{th}} \text{ item} \\&= \text{Size of } [3]^{\text{th}} \text{ item}\end{aligned}$$

$$Q_1 = 407$$

$$\begin{aligned}Q_3 &= \text{Size of } 3 \left[\frac{n+1}{4} \right]^{\text{th}} \text{ item} \\&= \text{Size of } 3 \left[\frac{11+1}{4} \right]^{\text{th}} \text{ item} \\&= \text{Size of } 3 \left[\frac{12}{4} \right]^{\text{th}} \text{ item} \\&= \text{Size of } 3 [3]^{\text{th}} \text{ item} \\&= \text{Size of } [9]^{\text{th}} \text{ item}\end{aligned}$$

$$Q_3 = 753$$

Quartile deviation is,

$$\begin{aligned}Q.D &= \frac{Q_3 - Q_1}{2} \\&= \frac{753 - 407}{2} \\&= \frac{346}{2} = 173\end{aligned}$$

$$\begin{aligned}\text{Coefficient of Q.D} &= \frac{Q_3 - Q_1}{Q_3 + Q_1} = \frac{753 - 407}{753 + 407} \\&= \frac{346}{1160} = 0.29\end{aligned}$$



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$$\text{Coefficient of Q.D} = \frac{Q_3 - Q_1}{Q_3 + Q_1} = \frac{753 - 407}{753 + 407}$$

$$\text{Coefficient of Q.D} = 0.29 = \frac{346}{1160} = 0.29$$